

Work each of the following problems. SHOW ALL WORK.

1. Nuclear fission that is not spontaneous starts by a neutron being captured by an unstable nucleus. Protons have nearly identical masses to neutrons. Protons and neutrons have nearly identical masses.

Neutrons have no charge and, unlike a proton, would not be repelled by a positively charged nucleus.

2. When heavy nuclei undergo fission, mass is lost. Where does this mass go?

The mass turns into energy that is released in a nuclear fission reaction.

3. One ton of TNT releases 4.18 gigajoules of energy. The metric prefix giga means billion. How much mass could be converted to energy to release this much energy?

$$E = \Delta mc^2$$

$$4.18 \times 10^9 \text{ J} = m(3 \times 10^8 \text{ m/s})^2$$

$$4.18 \times 10^9 \text{ J} = m(9 \times 10^{16} \text{ m}^2/\text{s}^2)$$

$$4.64 \times 10^{-8} \text{ kg} = m$$

4. How much energy is equivalent to 1 kilogram of mass?

$$E = \Delta mc^2$$

$$E = (1 \text{ kg})(3 \times 10^8 \text{ m/s})^2$$

$$E = (1 \text{ kg})(9 \times 10^{16} \text{ m}^2/\text{s}^2)$$

$$E = 9 \times 10^{16} \text{ J}$$

5. If the mass lost in a nuclear fission reaction is 0.50 grams, how much energy is released?

$$E = \Delta mc^2$$

$$E = (5 \times 10^{-4} \text{ kg})(3 \times 10^8 \text{ m/s})^2$$

$$E = (5 \times 10^{-4} \text{ kg})(9 \times 10^{16} \text{ m}^2/\text{s}^2)$$

$$E = 4.5 \times 10^{13} \text{ J}$$

Work each of the following problems. **SHOW ALL WORK.**

6. An electron has a mass of 9.12×10^{-31} kilograms. How much energy would be released if the mass of one electron was lost in a nuclear fission reaction?

$$E = \Delta mc^2$$

$$E = (9.12 \times 10^{-31} \text{ kg})(3 \times 10^8 \text{ m/s})^2$$

$$E = (9.12 \times 10^{-31} \text{ kg})(9 \times 10^{16} \text{ m}^2/\text{s}^2)$$

$$E = 8.21 \times 10^{-14} \text{ J}$$

7. The Little Boy atomic bomb released 63 terajoules of energy when it was dropped on Hiroshima, Japan. The metric prefix tera means 10^{12} times the base unit. How much mass was converted to energy during this explosion?

$$E = \Delta mc^2$$

$$6.3 \times 10^{13} \text{ J} = m(3 \times 10^8 \text{ m/s})^2$$

$$6.3 \times 10^{13} \text{ J} = m(9 \times 10^{16} \text{ m}^2/\text{s}^2)$$

$$m = 7.0 \times 10^{-4} \text{ kg}$$

8. The efficiency of nuclear reactors is 45%, meaning 45% of the energy created by nuclear fission turns into electricity. The highest producing nuclear power plant in 2015 created 11.63 billion kilowatt hours, which is equal to 4.18×10^{16} joules of energy. How much mass was converted at 45% efficiency to create this much energy?

$$E = \Delta mc^2$$

$$4.18 \times 10^{16} \text{ J} = m(3 \times 10^8 \text{ m/s})^2$$

$$4.18 \times 10^{16} \text{ J} = m(9 \times 10^{16} \text{ m}^2/\text{s}^2)$$

$$m = 0.464 \text{ kg}$$

This 0.464 kg is 45% of the actual amount of mass lost in the nuclear reactor. So, this mass

must be divided by 0.45 (45% as a decimal) to get the total amount of mass lost in the nuclear reactor.

$$mass_{total} = \frac{0.464 \text{ kg}}{0.45} = 1.031 \text{ kg}$$